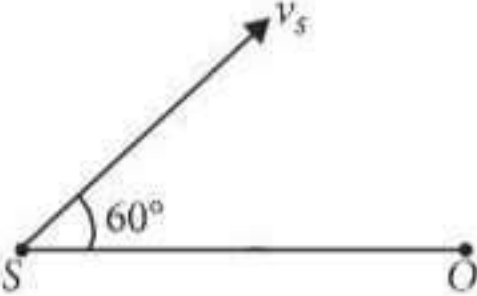


## Chapter 11. Waves

1. The two nearest harmonics of a tube closed at one end and open at other end are 220 Hz and 260 Hz. What is the fundamental frequency of the system?  
 (a) 20 Hz (b) 30 Hz  
 (c) 40 Hz (d) 10 Hz  
 (NEET 2017)
2. Two cars moving in opposite directions approach each other with speed of  $22 \text{ m s}^{-1}$  and  $16.5 \text{ m s}^{-1}$  respectively. The driver of the first car blows a horn having a frequency 400 Hz. The frequency heard by the driver of the second car is (velocity of sound is  $340 \text{ m s}^{-1}$ )  
 (a) 361 Hz (b) 411 Hz  
 (c) 448 Hz (d) 350 Hz  
 (NEET 2017)
3. The second overtone of an open organ pipe has the same frequency as the first overtone of a closed pipe  $L$  metre long. The length of the open pipe will be  
 (a)  $L$  (b)  $2L$   
 (c)  $\frac{L}{2}$  (d)  $4L$   
 (NEET-II 2016)
4. Three sound waves of equal amplitudes have frequencies  $(n-1)$ ,  $n$ ,  $(n+1)$ . They superimpose to give beats. The number of beats produced per second will be  
 (a) 1 (b) 4  
 (c) 3 (d) 2  
 (NEET-II 2016)
5. A siren emitting a sound of frequency 800 Hz moves away from an observer towards a cliff at a speed of  $15 \text{ m s}^{-1}$ . Then, the frequency of sound that the observer hears in the echo reflected from the cliff is  
 (Take velocity of sound in air =  $330 \text{ m s}^{-1}$ )  
 (a) 838 Hz (b) 885 Hz  
 (c) 765 Hz (d) 800 Hz  
 (NEET-I 2016)
6. An air column, closed at one end and open at the other, resonates with a tuning fork when the smallest length of the column is 50 cm. The next larger length of the column resonating with the same tuning fork is  
 (a) 150 cm (b) 200 cm  
 (c) 66.7 cm (d) 100 cm  
 (NEET-I 2016)
7. A uniform rope of length  $L$  and mass  $m_1$  hangs vertically from a rigid support. A block of mass  $m_2$  is attached to the free end of the rope. A transverse pulse of wavelength  $\lambda_1$  is produced at the lower end of the rope. The wavelength of the pulse when it reaches the top of the rope is  $\lambda_2$ . The ratio  $\lambda_2/\lambda_1$  is  
 (a)  $\sqrt{\frac{m_2}{m_1}}$  (b)  $\sqrt{\frac{m_1 + m_2}{m_1}}$   
 (c)  $\sqrt{\frac{m_1}{m_2}}$  (d)  $\sqrt{\frac{m_1 + m_2}{m_2}}$   
 (NEET-I 2016)
8. A string is stretched between fixed points separated by 75.0 cm. It is observed to have resonant frequencies of 420 Hz and 315 Hz. There are no other resonant frequencies between these two. The lowest resonant frequency for this string is  
 (a) 10.5 Hz (b) 105 Hz  
 (c) 155 Hz (d) 205 Hz  
 (2015)
9. 4.0 g of a gas occupies 22.4 litres at NTP. The specific heat capacity of the gas at constant volume is  $5.0 \text{ J K}^{-1} \text{ mol}^{-1}$ . If the speed of sound in this gas at NTP is  $952 \text{ m s}^{-1}$ , then the heat capacity at constant pressure is  
 (Take gas constant  $R = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$ )  
 (a)  $7.0 \text{ J K}^{-1} \text{ mol}^{-1}$  (b)  $8.5 \text{ J K}^{-1} \text{ mol}^{-1}$   
 (c)  $8.0 \text{ J K}^{-1} \text{ mol}^{-1}$  (d)  $7.5 \text{ J K}^{-1} \text{ mol}^{-1}$   
 (2015)

10. A source of sound  $S$  emitting waves of frequency 100 Hz and an observer  $O$  are located at some distance from each other. The source is moving with a speed of  $19.4 \text{ m s}^{-1}$  at an angle of  $60^\circ$  with the source observer line as shown in the figure. The observer is at rest. The apparent frequency observed by the observer (velocity of sound in air  $330 \text{ m s}^{-1}$ ), is
- 
- (a) 106 Hz (b) 97 Hz  
(c) 100 Hz (d) 103 Hz (2015)
11. The fundamental frequency of a closed organ pipe of length 20 cm is equal to the second overtone of an organ pipe open at both the ends. The length of organ pipe open at both the ends is
- (a) 120 cm (b) 140 cm  
(c) 80 cm (d) 100 cm (2015)
12. If  $n_1, n_2$  and  $n_3$  are the fundamental frequencies of three segments into which a string is divided, then the original fundamental frequency  $n$  of the string is given by
- (a)  $\frac{1}{n} = \frac{1}{n_1} + \frac{1}{n_2} + \frac{1}{n_3}$   
(b)  $\frac{1}{\sqrt{n}} = \frac{1}{\sqrt{n_1}} + \frac{1}{\sqrt{n_2}} + \frac{1}{\sqrt{n_3}}$   
(c)  $\sqrt{n} = \sqrt{n_1} + \sqrt{n_2} + \sqrt{n_3}$   
(d)  $n = n_1 + n_2 + n_3$  (2014)
13. The number of possible natural oscillations of air column in a pipe closed at one end of length 85 cm whose frequencies lie below 1250 Hz are (Velocity of sound =  $340 \text{ m s}^{-1}$ )
- (a) 4 (b) 5  
(c) 7 (d) 6 (2014)
14. A speeding motorcyclist sees traffic jam ahead him. He slows down to  $36 \text{ km hour}^{-1}$ . He finds that traffic has eased and a car moving ahead of him at  $18 \text{ km hour}^{-1}$  is honking at a frequency of 1392 Hz. If the speed of sound is  $343 \text{ m s}^{-1}$ , the frequency of the honk as heard by him will be
- (a) 1332 Hz (b) 1372 Hz  
(c) 1412 Hz (d) 1454 Hz (2014)

15. If we study the vibration of a pipe open at both ends, then the following statement is not true.
- (a) All harmonics of the fundamental frequency will be generated.  
(b) Pressure change will be maximum at both ends.  
(c) Open end will be antinode.  
(d) Odd harmonics of the fundamental frequency will be generated. (NEET 2013)
16. A wave travelling in the +ve  $x$ -direction having displacement along  $y$ -direction as 1 m, wavelength  $2\pi \text{ m}$  and frequency of  $\frac{1}{\pi} \text{ Hz}$  is represented by
- (a)  $y = \sin(10\pi x - 20\pi t)$   
(b)  $y = \sin(2\pi x + 2\pi t)$   
(c)  $y = \sin(x - 2t)$   
(d)  $y = \sin(2\pi x - 2\pi t)$  (NEET 2013)
17. A source of unknown frequency gives 4 beats/s when sounded with a source of known frequency 250 Hz. The second harmonic of the source of unknown frequency gives five beats per second, when sounded with a source of frequency 513 Hz. The unknown frequency is
- (a) 240 Hz (b) 260 Hz  
(c) 254 Hz (d) 246 Hz (NEET 2013)
18. The length of the wire between two ends of a sonometer is 100 cm. What should be the positions of two bridges below the wire so that the three segments of the wire have their fundamental frequencies in the ratio 1 : 3 : 5.
- (a)  $\frac{1500}{23} \text{ cm}, \frac{500}{23} \text{ cm}$   
(b)  $\frac{1500}{23} \text{ cm}, \frac{300}{23} \text{ cm}$   
(c)  $\frac{300}{23} \text{ cm}, \frac{1500}{23} \text{ cm}$   
(d)  $\frac{1500}{23} \text{ cm}, \frac{2000}{23} \text{ cm}$  (Karnataka NEET 2013)
19. Two sources  $P$  and  $Q$  produce notes of frequency 660 Hz each. A listener moves from  $P$  to  $Q$  with a speed of  $1 \text{ m s}^{-1}$ . If the speed of sound is  $330 \text{ m/s}$ , then the number of beats heard by the listener per second will be
- (a) 4 (b) 8  
(c) 2 (d) zero (Karnataka NEET 2013)

20. When a string is divided into three segments of length  $l_1$ ,  $l_2$  and  $l_3$  the fundamental frequencies of these three segments are  $v_1$ ,  $v_2$  and  $v_3$  respectively. The original fundamental frequency ( $v$ ) of the string is
- (a)  $\sqrt{v} = \sqrt{v_1} + \sqrt{v_2} + \sqrt{v_3}$   
 (b)  $v = v_1 + v_2 + v_3$   
 (c)  $\frac{1}{v} = \frac{1}{v_1} + \frac{1}{v_2} + \frac{1}{v_3}$   
 (d)  $\frac{1}{\sqrt{v}} = \frac{1}{\sqrt{v_1}} + \frac{1}{\sqrt{v_2}} + \frac{1}{\sqrt{v_3}}$  (2012)
21. Two sources of sound placed close to each other, are emitting progressive waves given by  $y_1 = 4\sin 600\pi t$  and  $y_2 = 5\sin 608\pi t$ . An observer located near these two sources of sound will hear
- (a) 4 beats per second with intensity ratio 25 : 16 between waxing and waning.  
 (b) 8 beats per second with intensity ratio 25 : 16 between waxing and waning.  
 (c) 8 beats per second with intensity ratio 81 : 1 between waxing and waning.  
 (d) 4 beats per second with intensity ratio 81 : 1 between waxing and waning. (2012)
22. The equation of a simple harmonic wave is given by
- $$y = 3 \sin \frac{\pi}{2} (50t - x),$$
- where  $x$  and  $y$  are in metres and  $t$  is in seconds. The ratio of maximum particle velocity to the wave velocity is
- (a)  $2\pi$  (b)  $\frac{3}{2}\pi$   
 (c)  $3\pi$  (d)  $\frac{2}{3}\pi$  (Mains 2012)
23. A train moving at a speed of  $220 \text{ m s}^{-1}$  towards a stationary object, emits a sound of frequency  $1000 \text{ Hz}$ . Some of the sound reaching the object gets reflected back to the train as echo. The frequency of the echo as detected by the driver of the train is  
 (Speed of sound in air is  $330 \text{ m s}^{-1}$ )
- (a)  $3500 \text{ Hz}$  (b)  $4000 \text{ Hz}$   
 (c)  $5000 \text{ Hz}$  (d)  $3000 \text{ Hz}$  (Mains 2012)
24. Two waves are represented by the equations  $y_1 = a\sin(\omega t + kx + 0.57) \text{ m}$  and  $y_2 = a\cos(\omega t + kx) \text{ m}$ , where  $x$  is in meter and  $t$  in sec. The phase difference between them is
- (a) 1.0 radian (b) 1.25 radian  
 (c) 1.57 radian (d) 0.57 radian (2011)
25. Sound waves travel at  $350 \text{ m/s}$  through a warm air and at  $3500 \text{ m/s}$  through brass. The wavelength of a  $700 \text{ Hz}$  acoustic wave as it enters brass from warm air
- (a) decrease by a factor 10  
 (b) increase by a factor 20  
 (c) increase by a factor 10  
 (d) decrease by a factor 20 (2011)
26. Two identical piano wires, kept under the same tension  $T$  have a fundamental frequency of  $600 \text{ Hz}$ . The fractional increase in the tension of one of the wires which will lead to occurrence of 6 beats/s when both the wires oscillate together would be
- (a) 0.01 (b) 0.02  
 (c) 0.03 (d) 0.04 (Mains 2011)
27. A transverse wave is represented by  $y = A\sin(\omega t - kx)$ . For what value of the wavelength is the wave velocity equal to the maximum particle velocity?
- (a)  $\pi A/2$  (b)  $\pi A$   
 (c)  $2\pi A$  (d)  $A$  (2010)
28. A tuning fork of frequency  $512 \text{ Hz}$  makes 4 beats per second with the vibrating string of a piano. The beat frequency decreases to 2 beats per sec when the tension in the piano string is slightly increased. The frequency of the piano string before increasing the tension was
- (a)  $510 \text{ Hz}$  (b)  $514 \text{ Hz}$   
 (c)  $516 \text{ Hz}$  (d)  $508 \text{ Hz}$  (2010)
29. Each of the two strings of length  $51.6 \text{ cm}$  and  $49.1 \text{ cm}$  are tensioned separately by  $20 \text{ N}$  force. Mass per unit length of both the strings is same and equal to  $1 \text{ g/m}$ . When both the strings vibrate simultaneously the number of beats is
- (a) 7 (b) 8  
 (c) 3 (d) 5 (2009)
30. The driver of a car travelling with speed  $30 \text{ m/s}$  towards a hill sounds a horn of frequency  $600 \text{ Hz}$ . If the velocity of sound in air is  $330 \text{ m/s}$ , the frequency of reflected sound as heard by driver is
- (a)  $555.5 \text{ Hz}$  (b)  $720 \text{ Hz}$   
 (c)  $500 \text{ Hz}$  (d)  $550 \text{ Hz}$  (2009)
31. A wave in a string has an amplitude of  $2 \text{ cm}$ . The wave travels in the +ve direction of  $x$  axis with a speed of  $128 \text{ m/s}$ , and it is noted that 5 complete waves fit in  $4 \text{ m}$  length of the string.

- The equation describing the wave is  
 (a)  $y = (0.02) \text{ m sin } (15.7 x - 2010t)$   
 (b)  $y = (0.02) \text{ m sin } (15.7 x + 2010t)$   
 (c)  $y = (0.02) \text{ m sin } (7.85 x - 1005t)$   
 (d)  $y = (0.02) \text{ m sin } (7.85 x + 1005t)$  (2009)
32. A point performs simple harmonic oscillation of period  $T$  and the equation of motion is given by  $x = a \sin(\omega t + \pi/6)$ . After the elapse of what fraction of the time period the velocity of the point will be equal to half of its maximum velocity?  
 (a)  $T/3$  (b)  $T/12$   
 (c)  $T/8$  (d)  $T/6$  (2008)
33. Two periodic waves of intensities  $I_1$  and  $I_2$  pass through a region at the same time in the same direction. The sum of the maximum and minimum intensities is  
 (a)  $(\sqrt{I_1} - \sqrt{I_2})^2$  (b)  $2(I_1 + I_2)$   
 (c)  $I_1 + I_2$  (d)  $(\sqrt{I_1} + \sqrt{I_2})^2$  (2008)
34. The wave described by  $y = 0.25 \sin(10\pi x - 2\pi t)$ , where  $x$  and  $y$  are in meters and  $t$  in seconds, is a wave travelling along the  
 (a) +ve  $x$  direction with frequency 1 Hz and wavelength  $\lambda = 0.2$  m.  
 (b) -ve  $x$  direction with amplitude 0.25 m and wavelength  $\lambda = 0.2$  m.  
 (c) -ve  $x$  direction with frequency 1 Hz.  
 (d) +ve  $x$  direction with frequency  $\pi$  Hz and wavelength  $\lambda = 0.2$  m. (2008)
35. Two vibrating tuning forks produce waves given by  $y_1 = 4 \sin 500\pi t$  and  $y_2 = 2 \sin 506 \pi t$ . Number of beats produced per minute is  
 (a) 360 (b) 180  
 (c) 60 (d) 3 (2006)
36. Two sound waves with wavelengths 5.0 m and 5.5 m respectively, each propagate in a gas with velocity 330 m/s. We expect the following number of beats per second.  
 (a) 6 (b) 12  
 (c) 0 (d) 1. (2006)
37. The time of reverberation of a room  $A$  is one second. What will be the time (in seconds) of reverberation of a room, having all the dimensions double of those of room  $A$ ?  
 (a) 1 (b) 2  
 (c) 4 (d) 1/2. (2006)
38. A transverse wave propagating along  $x$ -axis is represented by  $y(x, t) = 8.0 \sin(0.5\pi x - 4\pi t - \pi/4)$  where  $x$  is in metres and  $t$  is in seconds. The speed of the wave is  
 (a) 8 m/s (b)  $4\pi$  m/s  
 (c)  $0.5\pi$  m/s (d)  $\pi/4$  m/s. (2006)
39. Which one of the following statements is true?  
 (a) both light and sound waves can travel in vacuum  
 (b) both light and sound waves in air are transverse  
 (c) the sound waves in air are longitudinal while the light waves are transverse  
 (d) both light and sound waves in air are longitudinal. (2006)
40. A point source emits sound equally in all directions in a non-absorbing medium. Two points  $P$  and  $Q$  are at distances of 2 m and 3 m respectively from the source. The ratio of the intensities of the waves at  $P$  and  $Q$  is  
 (a) 3 : 2 (b) 2 : 3  
 (c) 9 : 4 (d) 4 : 9. (2005)
41. The phase difference between two waves, represented by  
 $y_1 = 10^{-6} \sin[100t + (x/50) + 0.5]$  m  
 $y_2 = 10^{-6} \cos[100t + (x/50)]$  m,  
 where  $x$  is expressed in metres and  $t$  is expressed in seconds, is approximately.  
 (a) 1.07 radians (b) 2.07 radians  
 (c) 0.5 radians (d) 1.5 radians (2004)
42. A car is moving towards a high cliff. The driver sounds a horn of frequency  $f$ . The reflected sound heard by the driver has frequency  $2f$ . If  $v$  is the velocity of sound, then the velocity of the car, in the same velocity units, will be  
 (a)  $v/\sqrt{2}$  (b)  $v/3$   
 (c)  $v/4$  (d)  $v/2$  (2004)
43. An observer moves towards a stationary source of sound with a speed  $1/5^{\text{th}}$  of the speed of sound. The wavelength and frequency of the source emitted are  $\lambda$  and  $f$  respectively. The apparent frequency and wavelength recorded by the observer are respectively  
 (a)  $1.2 f, 1.2 \lambda$  (b)  $1.2 f, \lambda$   
 (c)  $f, 1.2 \lambda$  (d)  $0.8 f, 0.8 \lambda$  (2003)
44. A whistle revolves in a circle with angular speed  $\omega = 20$  rad/s using a string of length 50 cm. If the frequency of sound from the whistle is 385 Hz, then what is the minimum frequency

- heard by an observer which is far away from the centre (velocity of sound = 340 m/s)  
 (a) 385 Hz (b) 374 Hz  
 (c) 394 Hz (d) 333 Hz. (2002)
45. A wave travelling in positive  $X$ -direction with  $a = 0.2 \text{ ms}^{-2}$ , velocity =  $360 \text{ ms}^{-1}$  and  $\lambda = 60 \text{ m}$ , then correct expression for the wave is  
 (a)  $y = 0.2 \sin \left[ 2\pi \left( 6t + \frac{x}{60} \right) \right]$   
 (b)  $y = 0.2 \sin \left[ \pi \left( 6t + \frac{x}{60} \right) \right]$   
 (c)  $y = 0.2 \sin \left[ 2\pi \left( 6t - \frac{x}{60} \right) \right]$   
 (d)  $y = 0.2 \sin \left[ \pi \left( 6t - \frac{x}{60} \right) \right]$  (2002)
46. The equation of a wave is represented by  $y = 10^{-4} \sin \left( 100t - \frac{x}{10} \right) \text{ m}$ , then the velocity of wave will be  
 (a) 100 m/s (b) 4 m/s  
 (c) 1000 m/s (d) 10 m/s (2001)
47. Two waves having equation  $x_1 = a \sin(\omega t - kx + \phi_1)$ ,  $x_2 = a \sin(\omega t - kx + \phi_2)$ . If in the resultant wave the frequency and amplitude remain equal to amplitude of superimposing waves, the phase difference between them is  
 (a)  $\frac{\pi}{6}$  (b)  $\frac{2\pi}{3}$   
 (c)  $\frac{\pi}{4}$  (d)  $\frac{\pi}{3}$ . (2001)
48. If the tension and diameter of a sonometer wire of fundamental frequency  $n$  is doubled and density is halved then its fundamental frequency will become  
 (a)  $\frac{n}{4}$  (b)  $\sqrt{2}n$   
 (c)  $n$  (d)  $\frac{n}{\sqrt{2}}$ . (2001)
49. The equations of two waves acting in perpendicular directions are given as  $x = a \cos(\omega t + \delta)$  and  $y = a \cos(\omega t + \alpha)$ , where  $\delta = \alpha + \frac{\pi}{2}$ , the resultant wave represents  
 (a) a parabola (b) a circle  
 (c) an ellipse (d) a straight line (2000)
50. A string is cut into three parts, having fundamental frequencies  $n_1, n_2, n_3$  respectively. Then original fundamental frequency  $n$  related by the expression as  
 (a)  $\frac{1}{n} = \frac{1}{n_1} + \frac{1}{n_2} + \frac{1}{n_3}$  (b)  $n = n_1 \times n_2 \times n_3$   
 (c)  $n = n_1 + n_2 + n_3$  (d)  $n = \frac{n_1 + n_2 + n_3}{3}$ . (2000)
51. Two stationary sources each emitting waves of wavelength  $\lambda$ , an observer moves from one source to another with velocity  $u$ . Then number of beats heard by him  
 (a)  $\frac{2u}{\lambda}$  (b)  $\frac{u}{\lambda}$   
 (c)  $\sqrt{u\lambda}$  (d)  $\frac{u}{2\lambda}$  (2000)
52. Two waves of lengths 50 cm and 51 cm produced 12 beats per sec. The velocity of sound is  
 (a) 340 m/s (b) 331 m/s  
 (c) 306 m/s (d) 360 m/s (1999)
53. A transverse wave is represented by the equation  $y = y_0 \sin \frac{2\pi}{\lambda} (vt - x)$ . For what value of  $\lambda$ , is the maximum particle velocity equal to two times the wave velocity?  
 (a)  $\lambda = \frac{\pi y_0}{2}$  (b)  $\lambda = \frac{\pi y_0}{3}$   
 (c)  $\lambda = 2\pi y_0$  (d)  $\lambda = \pi y_0$  (1998)
54. A vehicle, with a horn of frequency  $n$  is moving with a velocity of 30 m/s in a direction perpendicular to the straight line joining the observer and the vehicle. The observer perceives the sound to have a frequency  $n + n_1$ . Then (if the sound velocity in air is 300 m/s)  
 (a)  $n_1 = 0.1n$  (b)  $n_1 = 0$   
 (c)  $n_1 = 10n$  (d)  $n_1 = -0.1n$  (1998)
55. A standing wave having 3 nodes and 2 antinodes is formed between two atoms having a distance 1.21 Å between them. The wavelength of the standing wave is  
 (a) 6.05 Å (b) 2.42 Å  
 (c) 1.21 Å (d) 3.63 Å (1998)
56. In a sinusoidal wave, the time required for a particular point to move from maximum displacement to zero displacement is 0.170 s. The frequency of wave is  
 (a) 0.73 Hz (b) 0.36 Hz  
 (c) 1.47 Hz (d) 2.94 Hz (1998)



57. Standing waves are produced in 10 m long stretched string. If the string vibrates in 5 segments and wave velocity is 20 m/s, the frequency is  
 (a) 5 Hz (b) 10 Hz  
 (c) 2 Hz (d) 4 Hz (1997)
58. A cylindrical tube, open at both ends has fundamental frequency  $f$  in air. The tube is dipped vertically in water, so that half of it is in water. The fundamental frequency of air column is now  
 (a)  $f/2$  (b)  $3f/4$   
 (c)  $2f$  (d)  $f$  (1997)
59. The equation of a sound wave is  $y = 0.0015 \sin(62.4x + 316t)$ . The wavelength of this wave is  
 (a) 0.3 unit (b) 0.2 unit  
 (c) 0.1 unit (d) cannot be calculated. (1996)
60. Two sound waves having a phase difference of  $60^\circ$  have path difference of  
 (a)  $\frac{\lambda}{6}$  (b)  $\frac{\lambda}{3}$   
 (c)  $2\lambda$  (d)  $\frac{\lambda}{2}$  (1996)
61. The length of a sonometer wire  $AB$  is 110 cm. Where should the two bridges be placed from  $A$  to divide the wire in 3 segments whose fundamental frequencies are in the ratio of 1 : 2 : 3?  
 (a) 60 cm and 90 cm  
 (b) 30 cm and 60 cm  
 (c) 30 cm and 90 cm  
 (d) 40 cm and 80 cm. (1995)
62. A hospital uses an ultrasonic scanner to locate tumours in a tissue. The operating frequency of the scanner is 4.2 MHz. The speed of sound in a tissue is 1.7 km/s. The wavelength of sound in the tissue is close to  
 (a)  $4 \times 10^{-3}$  m (b)  $8 \times 10^{-3}$  m  
 (c)  $4 \times 10^{-4}$  m (d)  $8 \times 10^{-4}$  m. (1995)
63. A source of sound gives 5 beats per second, when sounded with another source of frequency  $100 \text{ second}^{-1}$ . The second harmonic of the source, together with a source of frequency  $205 \text{ sec}^{-1}$  gives 5 beats per second. What is the frequency of the source?  
 (a)  $105 \text{ second}^{-1}$  (b)  $205 \text{ second}^{-1}$   
 (c)  $95 \text{ second}^{-1}$  (d)  $100 \text{ second}^{-1}$  (1995)
64. A star, which is emitting radiation at a wavelength of 5000 Å, is approaching the earth with a velocity of  $1.5 \times 10^4 \text{ m/s}$ . The change in wavelength of the radiation as received on the earth is  
 (a) 25 Å (b) 100 Å  
 (c) zero (d) 2.5 Å (1995)
65. Which one of the following represents a wave?  
 (a)  $y = A \sin(\omega t - kx)$   
 (b)  $y = A \cos(at - bx + c)$   
 (c)  $y = A \sin kx$   
 (d)  $y = A \sin \omega t$ . (1994)
66. A wave of frequency 100 Hz travels along a string towards its fixed end. When this wave travels back, after reflection, a node is formed at a distance of 10 cm from the fixed end. The speed of the wave (incident and reflected) is  
 (a) 20 m/s (b) 40 m/s  
 (c) 5 m/s (d) 10 m/s. (1994)
67. A stationary wave is represented by  $y = A \sin(100t) \cos(0.01x)$ , where  $y$  and  $A$  are in millimetres,  $t$  is in seconds and  $x$  is in metres. The velocity of the wave is  
 (a)  $10^4 \text{ m/s}$  (b) not derivable  
 (c) 1 m/s (d)  $10^2 \text{ m/s}$ . (1994)
68. A source of frequency  $\nu$  gives 5 beats/second when sounded with a source of frequency 200 Hz. The second harmonic of frequency  $2\nu$  of source gives 10 beats/second when sounded with a source of frequency 420 Hz. The value of  $\nu$  is  
 (a) 205 Hz (b) 195 Hz  
 (c) 200 Hz (d) 210 Hz. (1994)
69. Wave has simple harmonic motion whose period is 4 seconds while another wave which also possesses simple harmonic motion has its period 3 second. If both are combined, then the resultant wave will have the period equal to  
 (a) 4 s (b) 5 s  
 (c) 12 s (d) 3 s (1993)
70. A stretched string resonates with tuning fork frequency 512 Hz when length of the string is 0.5 m. The length of the string required to vibrate resonantly with a tuning fork of frequency 256 Hz would be  
 (a) 0.25 m (b) 0.5 m  
 (c) 1 m (d) 2 m (1993)
71. The temperature at which the speed of sound becomes double as was at  $27^\circ\text{C}$  is  
 (a)  $273^\circ\text{C}$  (b)  $0^\circ\text{C}$   
 (c)  $927^\circ\text{C}$  (d)  $1027^\circ\text{C}$  (1993)

72. For production of beats the two sources must have  
 (a) different frequencies and same amplitude  
 (b) different frequencies  
 (c) different frequencies, same amplitude and same phase  
 (d) different frequencies and same phase (1992)
73. The frequency of sinusoidal wave  $y = 0.40\cos [2000t + 0.80]$  would be  
 (a)  $1000\pi$  Hz (b) 2000 Hz  
 (c) 20 Hz (d)  $\frac{1000}{\pi}$  Hz (1992)
74. With the propagation of a longitudinal wave through a material medium, the quantities transmitted in the propagation direction are  
 (a) energy, momentum and mass  
 (b) energy  
 (c) energy and mass  
 (d) energy and linear momentum (1992)
75. Two trains move towards each other with the same speed. The speed of sound is 340 m/s. If the height of the tone of the whistle of one of them heard on the other changes to  $\frac{9}{8}$  times, then the speed of each train should be  
 (a) 20 m/s (b) 2 m/s  
 (c) 200 m/s (d) 2000 m/s (1991)
76. A closed organ pipe (closed at one end) is excited to support the third overtone. It is found that air in the pipe has  
 (a) three nodes and three antinodes  
 (b) three nodes and four antinodes  
 (c) four nodes and three antinodes  
 (d) four nodes and four antinodes (1991)
77. Velocity of sound waves in air is 330 m/s. For a particular sound wave in air, a path difference of 40 cm is equivalent to phase difference of  $1.6\pi$ . The frequency of this wave is  
 (a) 165 Hz (b) 150 Hz  
 (c) 660 Hz (d) 330 Hz (1990)
78. A 5.5 metre length of string has a mass of 0.035 kg. If the tension in the string is 77 N, the speed of a wave on the string is  
 (a)  $110\text{ m s}^{-1}$  (b)  $165\text{ m s}^{-1}$   
 (c)  $77\text{ m s}^{-1}$  (d)  $102\text{ m s}^{-1}$  (1989)
79. If the amplitude of sound is doubled and the frequency reduced to one fourth, the intensity of sound at the same point will be  
 (a) increasing by a factor of 2  
 (b) decreasing by a factor of 2  
 (c) decreasing by a factor of 4  
 (d) unchanged (1989)
80. The velocity of sound in any gas depends upon  
 (a) wavelength of sound only  
 (b) density and elasticity of gas  
 (c) intensity of sound waves only  
 (d) amplitude and frequency of sound (1988)
81. Equation of progressive wave is given by  $y = 4\sin\left[\pi\left(\frac{t}{5} - \frac{x}{9}\right) + \frac{\pi}{6}\right]$  where  $y, x$  are in cm and  $t$  is in seconds. Then which of the following is correct?  
 (a)  $v = 5\text{ cm}$  (b)  $\lambda = 18\text{ cm}$   
 (c)  $a = 0.04\text{ cm}$  (d)  $f = 50\text{ Hz}$  (1988)

### Answer Key

- |         |         |         |         |           |         |         |         |         |         |
|---------|---------|---------|---------|-----------|---------|---------|---------|---------|---------|
| 1. (a)  | 2. (c)  | 3. (b)  | 4. (d)  | 5. (a)    | 6. (a)  | 7. (d)  | 8. (b)  | 9. (c)  | 10. (d) |
| 11. (a) | 12. (a) | 13. (d) | 14. (c) | 15. (b)   | 16. (c) | 17. (c) | 18. (d) | 19. (a) | 20. (c) |
| 21. (d) | 22. (b) | 23. (c) | 24. (a) | 25. (c)   | 26. (b) | 27. (c) | 28. (d) | 29. (a) | 30. (b) |
| 31. (c) | 32. (b) | 33. (b) | 34. (a) | 35. (b)   | 36. (a) | 37. (b) | 38. (a) | 39. (c) | 40. (c) |
| 41. (a) | 42. (b) | 43. (b) | 44. (b) | 45. (c)   | 46. (c) | 47. (b) | 48. (c) | 49. (b) | 50. (a) |
| 51. (a) | 52. (c) | 53. (d) | 54. (b) | 55. (c)   | 56. (c) | 57. (a) | 58. (d) | 59. (c) | 60. (a) |
| 61. (a) | 62. (c) | 63. (a) | 64. (a) | 65. (a,b) | 66. (a) | 67. (a) | 68. (a) | 69. (c) | 70. (c) |
| 71. (c) | 72. (b) | 73. (d) | 74. (b) | 75. (a)   | 76. (d) | 77. (c) | 78. (a) | 79. (c) | 80. (b) |
| 81. (b) |         |         |         |           |         |         |         |         |         |

## EXPLANATIONS

1. (a) : Nearest harmonics of an organ pipe closed at one end differ by twice of its fundamental frequency.

$$\therefore 260 - 220 = 2v, v = 20 \text{ Hz}$$

2. (c) : The required frequency of sound heard by the driver of second car is given as

$$v' = v \left( \frac{v + v_o}{v - v_s} \right),$$

where  $v$  = velocity of sound

$v_o$  = velocity of observer, i.e., second car

$v_s$  = velocity of source i.e., first car

$$v' = 400 \left( \frac{340 + 16.5}{340 - 22} \right) = 400 \left( \frac{356.5}{318} \right)$$

$$v' \approx 448 \text{ Hz}$$

3. (b) : Second overtone of an open organ pipe

$$\text{(Third harmonic)} = 3 \times v'_0 = 3 \times \frac{v}{2L'}$$

First overtone of a closed organ pipe

$$\text{(Third harmonic)} = 3 \times v_0 = 3 \times \frac{v}{4L}$$

According to question,

$$3v'_0 = 3v_0 \Rightarrow 3 \times \frac{v}{2L'} = 3 \times \frac{v}{4L}$$

$$\therefore L' = 2L$$

4. (d)

5. (a) : Here, frequency of sound emitted by siren,

$$v_0 = 800 \text{ Hz}$$

Speed of source,  $v_s = 15 \text{ m s}^{-1}$

Speed of sound in air,  $v = 330 \text{ m s}^{-1}$

Apparent frequency of sound at the cliff

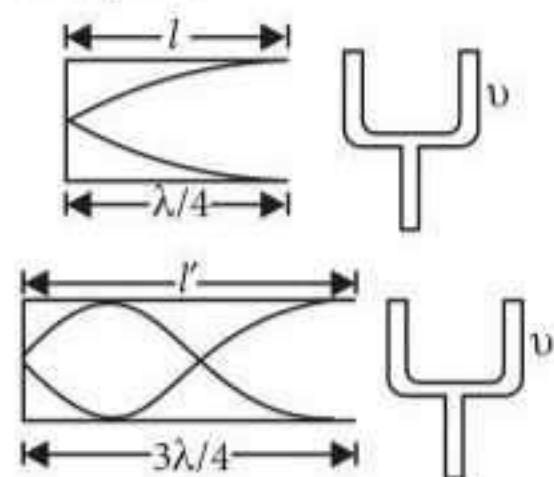
$$= \text{frequency heard by observer} = v$$

Using Doppler's effect of sound

$$v = \left( \frac{v}{v - v_s} \right) v_0 = \frac{330}{330 - 15} \times 800$$

$$= \frac{330}{315} \times 800 = 838.09 \text{ Hz} \approx 838 \text{ Hz}$$

6. (a) : From figure,



First harmonic is obtained at

$$l = \frac{\lambda}{4} = 50 \text{ cm}$$

Third harmonic is obtained for resonance,

$$l' = \frac{3\lambda}{4} = 3 \times 50 = 150 \text{ cm.}$$

7. (d) : Wavelength of pulse at the lower end,

$$\lambda_1 \propto \text{velocity } (v_1) = \sqrt{\frac{T_1}{\mu}}$$

$$\text{Similarly, } \lambda_2 \propto v_2 = \sqrt{\frac{T_2}{\mu}}$$

$$\therefore \frac{\lambda_2}{\lambda_1} = \sqrt{\frac{T_2}{T_1}} = \sqrt{\frac{(m_1 + m_2)g}{m_2g}}$$

$$= \sqrt{\frac{m_1 + m_2}{m_2}}$$



8. (b) : For a string fixed at both ends, the resonant frequencies are

$$v_n = \frac{nv}{2L} \text{ where } n = 1, 2, 3, \dots$$

The difference between two consecutive resonant frequencies is

$$\Delta v_n = v_{n+1} - v_n = \frac{(n+1)v}{2L} - \frac{nv}{2L} = \frac{v}{2L}$$

which is also the lowest resonant frequency ( $n = 1$ ).

Thus the lowest resonant frequency for the given string =  $420 \text{ Hz} - 315 \text{ Hz} = 105 \text{ Hz}$

9. (c) : Since 4.0 g of a gas occupies 22.4 litres at NTP, so the molecular mass of the gas is

$$M = 4.0 \text{ g mol}^{-1}$$

As the speed of the sound in the gas is

$$v = \sqrt{\frac{\gamma RT}{M}}$$

where  $\gamma$  is the ratio of two specific heats,  $R$  is the universal gas constant and  $T$  is the temperature of the gas.

$$\therefore \gamma = \frac{Mv^2}{RT}$$

Here,  $M = 4.0 \text{ g mol}^{-1} = 4.0 \times 10^{-3} \text{ kg mol}^{-1}$ ,

$v = 952 \text{ m s}^{-1}$ ,  $R = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$  and  $T = 273 \text{ K}$  (at NTP)

$$\therefore \gamma = \frac{(4.0 \times 10^{-3} \text{ kg mol}^{-1})(952 \text{ m s}^{-1})^2}{(8.3 \text{ J K}^{-1} \text{ mol}^{-1})(273 \text{ K})} = 1.6$$



By definition,  $\gamma = \frac{C_p}{C_v}$  or  $C_p = \gamma C_v$

But  $\gamma = 1.6$  and  $C_v = 5.0 \text{ JK}^{-1} \text{ mol}^{-1}$

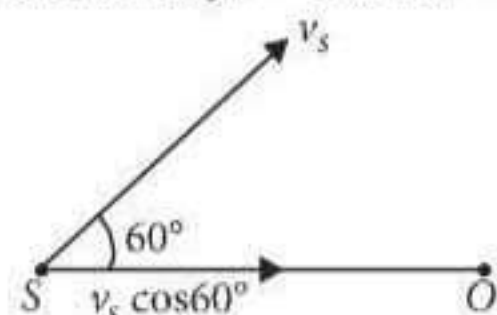
$$\therefore C_p = (1.6)(5.0 \text{ JK}^{-1} \text{ mol}^{-1}) = 8.0 \text{ JK}^{-1} \text{ mol}^{-1}$$

10. (d) : Here,

Frequency of source,  $\nu_0 = 100 \text{ Hz}$

Velocity of source,  $\nu_s = 19.4 \text{ ms}^{-1}$

Velocity of sound in air,  $\nu = 330 \text{ ms}^{-1}$



As the velocity of source along the source observer line is  $\nu_s \cos 60^\circ$  and the observer is at rest, so the apparent frequency observed by the observer is

$$\begin{aligned} \nu &= \nu_0 \left( \frac{\nu}{\nu - \nu_s \cos 60^\circ} \right) \\ &= (100 \text{ Hz}) \left( \frac{330 \text{ ms}^{-1}}{330 \text{ ms}^{-1} - (19.4 \text{ ms}^{-1}) \left( \frac{1}{2} \right)} \right) \\ &= (100 \text{ Hz}) \left( \frac{330 \text{ ms}^{-1}}{330 \text{ ms}^{-1} - 9.7 \text{ ms}^{-1}} \right) \\ &= (100 \text{ Hz}) \left( \frac{330 \text{ ms}^{-1}}{320.3 \text{ ms}^{-1}} \right) = 103 \text{ Hz} \end{aligned}$$

11. (a) : For closed organ pipe, fundamental frequency is given by  $\nu_c = \frac{\nu}{4l}$

For open organ pipe, fundamental frequency is given by  $\nu_o = \frac{\nu}{2l'}$

2<sup>nd</sup> overtone of open organ pipe

$$\nu' = 3\nu_o \quad \nu' = \frac{3\nu}{2l'}$$

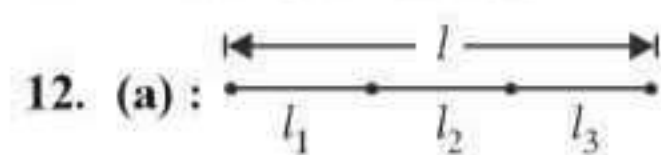
According to question,  $\nu_c = \nu'$

$$\frac{\nu}{4l} = \frac{3\nu}{2l'}$$

$$l' = 6l$$

Here,  $l = 20 \text{ cm}$ ,  $l' = ?$

$$\therefore l' = 6 \times 20 = 120 \text{ cm}$$



$$n_1 = \frac{1}{2l_1} \sqrt{\frac{T}{\mu}} \quad \dots(i)$$

$$n_2 = \frac{1}{2l_2} \sqrt{\frac{T}{\mu}} \quad \dots(ii)$$

$$n_3 = \frac{1}{2l_3} \sqrt{\frac{T}{\mu}} \quad \dots(iii)$$

$$n = \frac{1}{2l} \sqrt{\frac{T}{\mu}} \quad \dots(iv)$$

From eqn. (iv), we get

$$\frac{1}{n} = \frac{2l}{\sqrt{\frac{T}{\mu}}}$$

As  $l = l_1 + l_2 + l_3$

$$\begin{aligned} \therefore \frac{1}{n} &= \frac{2(l_1 + l_2 + l_3)}{\sqrt{\frac{T}{\mu}}} = \frac{2l_1}{\sqrt{\frac{T}{\mu}}} + \frac{2l_2}{\sqrt{\frac{T}{\mu}}} + \frac{2l_3}{\sqrt{\frac{T}{\mu}}} \\ &= \frac{1}{n_1} + \frac{1}{n_2} + \frac{1}{n_3} \quad [\text{Using (i), (ii) and (iii)}] \end{aligned}$$

13. (d) : Fundamental frequency of the closed organ pipe is

$$\nu = \frac{\nu}{4L}$$

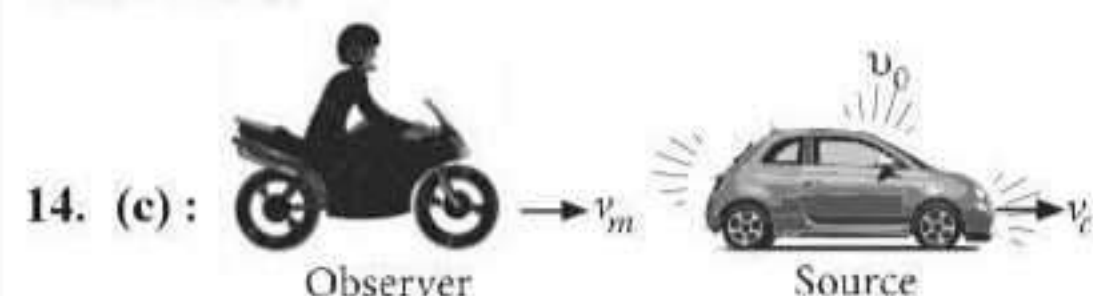
Here,  $\nu = 340 \text{ m s}^{-1}$ ,  $L = 85 \text{ cm} = 0.85 \text{ m}$

$$\therefore \nu = \frac{340 \text{ m s}^{-1}}{4 \times 0.85 \text{ m}} = 100 \text{ Hz}$$

The natural frequencies of the closed organ pipe will be

$$\begin{aligned} \nu_n &= (2n - 1)\nu = \nu, 3\nu, 5\nu, 7\nu, 9\nu, 11\nu, 13\nu, \dots \\ &= 100 \text{ Hz}, 300 \text{ Hz}, 500 \text{ Hz}, 700 \text{ Hz}, 900 \text{ Hz}, \\ &\quad 1100 \text{ Hz}, 1300 \text{ Hz}, \dots \text{ and so on} \end{aligned}$$

Thus, the natural frequencies lies below the 1250 Hz is 6.



Here, speed of motorcyclist,  $\nu_m = 36 \text{ km hour}^{-1}$   
 $= 36 \times \frac{5}{18} = 10 \text{ m s}^{-1}$

Speed of car,

$$\nu_c = 18 \text{ km hour}^{-1} = 18 \times \frac{5}{18} \text{ m s}^{-1} = 5 \text{ m s}^{-1}$$

Frequency of source,  $\nu_0 = 1392 \text{ Hz}$

Speed of sound,  $\nu = 343 \text{ m s}^{-1}$

The frequency of the honk heard by the motorcyclist is

$$\begin{aligned} \nu' &= \nu_0 \left( \frac{\nu + \nu_m}{\nu + \nu_c} \right) = 1392 \left( \frac{343 + 10}{343 + 5} \right) \\ &= \frac{1392 \times 353}{348} = 1412 \text{ Hz} \end{aligned}$$

15. (b) : Pressure change will be minimum at both ends.

16. (c) : The standard equation of a wave travelling along +ve x-direction is given by

$$y = A \sin(kx - \omega t)$$

where

$A$  = Amplitude of the wave

$k$  = angular wave number

$\omega$  = angular frequency of the wave

Given:  $A = 1$  m,  $\lambda = 2\pi$  m,  $\nu = \frac{1}{\pi}$  Hz

As  $k = \frac{2\pi}{\lambda} = \frac{2\pi}{2\pi} = 1$

$$\omega = 2\pi\nu = 2\pi \times \frac{1}{\pi} = 2$$

$\therefore$  The equation of the given wave is

$$y = 1 \sin(1x - 2t) = \sin(x - 2t)$$

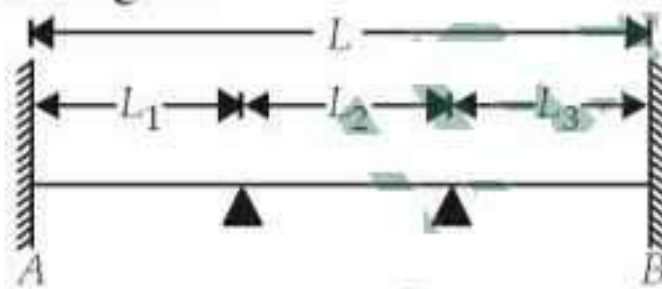
17. (c) : Let  $\nu$  be frequency of the unknown source. As it gives 4 beats per second when sounded with a source of frequency 250 Hz,

$$\therefore \nu = 250 \pm 4 = 246 \text{ Hz or } 254 \text{ Hz}$$

Second harmonic of this unknown source = 492 Hz or 508 Hz which gives 5 beats per second when sounded with a source of frequency 513 Hz.

Therefore unknown frequency,  $\nu = 254$  Hz.

18. (d) : Let  $L (= 100 \text{ cm})$  be the length of the wire and  $L_1, L_2$  and  $L_3$  are the lengths of the segments as shown in the figure.



Fundamental frequency,  $\nu \propto \frac{1}{L}$

As the fundamental frequencies are in the ratio of  $1 : 3 : 5$ ,

$$\therefore L_1 : L_2 : L_3 = \frac{1}{1} : \frac{1}{3} : \frac{1}{5} = 15 : 5 : 3$$

Let  $x$  be the common factor. Then

$$15x + 5x + 3x = L = 100$$

$$23x = 100 \text{ or } x = \frac{100}{23}$$

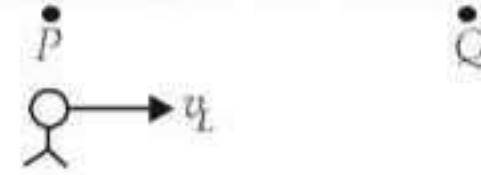
$$\therefore L_1 = 15 \times \frac{100}{23} = \frac{1500}{23} \text{ cm}$$

$$L_2 = 5 \times \frac{100}{23} = \frac{500}{23} \text{ cm}$$

$$L_3 = 3 \times \frac{100}{23} = \frac{300}{23} \text{ cm}$$

$\therefore$  The bridges should be placed from  $A$  at  $\frac{1500}{23}$  cm and  $\frac{2000}{23}$  cm respectively.

19. (a) : The situation as shown in the figure.



Here,

Speed of listener,  $\nu_L = 1 \text{ ms}^{-1}$

Speed of sound,  $\nu = 330 \text{ ms}^{-1}$

Frequency of each source,  $\nu = 660 \text{ Hz}$

Apparent frequency due to  $P$ ,

$$\nu' = \frac{\nu(\nu - \nu_L)}{\nu}$$

Apparent frequency due to  $Q$ ,

$$\nu'' = \frac{\nu(\nu + \nu_L)}{\nu}$$

Number of beats heard by the listener per second is

$$\begin{aligned} \nu'' - \nu' &= \frac{\nu(\nu + \nu_L)}{\nu} - \frac{\nu(\nu - \nu_L)}{\nu} \\ &= \frac{2\nu\nu_L}{\nu} = \frac{2 \times 660 \times 1}{330} = 4 \end{aligned}$$

20. (c) : Let  $l$  be the length of the string.

Fundamental frequency is given by

$$\nu = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$$

or  $\nu \propto \frac{1}{l}$  ( $\because T$  and  $\mu$  are constants)

Here,  $l_1 = \frac{k}{\nu_1}, l_2 = \frac{k}{\nu_2}, l_3 = \frac{k}{\nu_3}$  and  $l = \frac{k}{\nu}$

But  $l = l_1 + l_2 + l_3$

$$\therefore \frac{1}{\nu} = \frac{1}{\nu_1} + \frac{1}{\nu_2} + \frac{1}{\nu_3}$$

21. (d) : Given :  $y_1 = 4\sin 600\pi t, y_2 = 5\sin 608\pi t$

$\therefore \omega_1 = 600\pi$  or  $2\pi\nu_1 = 600\pi$  or  $\nu_1 = 300$

$$A_1 = 4$$

and  $\omega_2 = 608\pi$  or  $2\pi\nu_2 = 608\pi$  or  $\nu_2 = 304$

$$A_2 = 5$$

Number of beats heard per second

$$= \nu_2 - \nu_1 = 304 - 300 = 4$$

$$\frac{I_{\max}}{I_{\min}} = \frac{(A_1 + A_2)^2}{(A_1 - A_2)^2} = \frac{(4 + 5)^2}{(4 - 5)^2} = \frac{81}{1}$$

22. (b) : The given wave equation is

$$y = 3 \sin \frac{\pi}{2} (50t - x)$$

$$y = 3 \sin \left( 25\pi t - \frac{\pi}{2} x \right)$$

... (i)

The standard wave equation is

$$y = A \sin(\omega t - kx) \quad \dots(ii)$$

Comparing (i) and (ii), we get

$$\omega = 25\pi, \quad k = \frac{\pi}{2}$$

Wave velocity,

$$v = \frac{\omega}{k} = \frac{25\pi}{(\pi/2)} = 50 \text{ ms}^{-1}$$

$$\begin{aligned} \text{Particle velocity, } v_p &= \frac{dy}{dt} = \frac{d}{dt} \left( 3 \sin \left( 25\pi t - \frac{\pi}{2} \right) \right) \\ &= 75\pi \cos \left( 25\pi t - \frac{\pi}{2} \right) \end{aligned}$$

Maximum particle velocity,  $(v_p)_{\max} = 75\pi \text{ ms}^{-1}$

$$\therefore \frac{(v_p)_{\max}}{v} = \frac{75\pi}{50} = \frac{3}{2}\pi$$

23. (c) : Here,

Speed of the train,  $v_T = 220 \text{ ms}^{-1}$

Speed of sound in air,  $v = 330 \text{ ms}^{-1}$

The frequency of the echo detected by the driver of the train is

$$\begin{aligned} v' &= v \left( \frac{v + v_T}{v - v_T} \right) = 1000 \left( \frac{330 + 220}{330 - 220} \right) \\ &= 1000 \times \frac{550}{110} = 5000 \text{ Hz} \end{aligned}$$

24. (a) :  $y_1 = a \sin(\omega t + kx + 0.57)$

$\therefore$  Phase,  $\phi_1 = \omega t + kx + 0.57$

$$y_2 = a \cos(\omega t + kx) = a \sin \left( \omega t + kx + \frac{\pi}{2} \right)$$

$\therefore$  Phase,  $\phi_2 = \omega t + kx + \frac{\pi}{2}$

Phase difference,  $\Delta\phi = \phi_2 - \phi_1$

$$\begin{aligned} &= \left( \omega t + kx + \frac{\pi}{2} \right) - (\omega t + kx + 0.57) = \frac{\pi}{2} - 0.57 \\ &= (1.57 - 0.57) \text{ radian} = 1 \text{ radian} \end{aligned}$$

25. (c) : Here,  $v_{\text{air}} = 350 \text{ m/s}$ ,  $v_{\text{brass}} = 3500 \text{ m/s}$

When a sound wave travels from one medium to another medium its frequency remains the same

$\therefore$  Frequency,  $v = \frac{v}{\lambda}$

Since  $v$  remains the same in both the medium

$$\Rightarrow \frac{v_{\text{air}}}{\lambda_{\text{air}}} = \frac{v_{\text{brass}}}{\lambda_{\text{brass}}}$$

$$\lambda_{\text{brass}} = \lambda_{\text{air}} \times \frac{v_{\text{brass}}}{v_{\text{air}}} = \lambda_{\text{air}} \times \frac{3500}{350} = 10\lambda_{\text{air}}$$

26. (b) : As  $v = \frac{1}{2L} \sqrt{\frac{T}{\mu}} \therefore \frac{\Delta v}{v} = \frac{1}{2} \frac{\Delta T}{T}$

$$\frac{\Delta T}{T} = 2 \frac{\Delta v}{v} = 2 \times \frac{6}{600} = 0.02$$

27. (c) : The given wave equation is

$$y = A \sin(\omega t - kx)$$

Wave velocity,  $v = \frac{\omega}{k} \quad \dots(i)$

Particle velocity,  $v_p = \frac{dy}{dt} = A\omega \cos(\omega t - kx)$

Maximum particle velocity,  $(v_p)_{\max} = A\omega \quad \dots(ii)$

According to the given question

$$v = (v_p)_{\max}$$

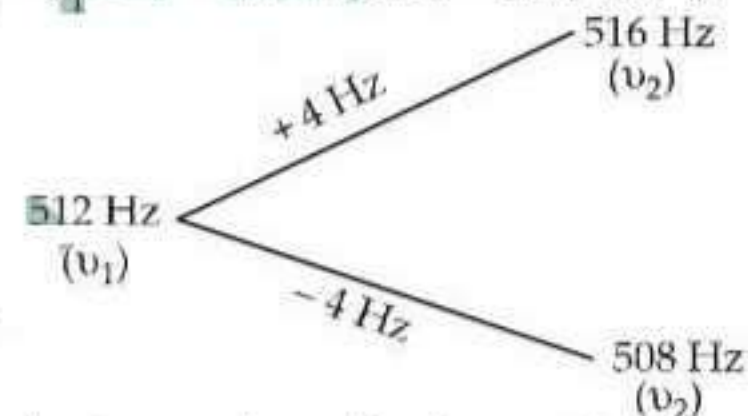
$$\frac{\omega}{k} = A\omega \quad \text{(Using (i) and (ii))}$$

$$\frac{1}{k} = A \quad \text{or} \quad \frac{\lambda}{2\pi} = A \quad \left( \because k = \frac{2\pi}{\lambda} \right)$$

$$\lambda = 2\pi A$$

28. (d) : Let the frequencies of tuning fork and piano string be  $v_1$  and  $v_2$  respectively.

$\therefore v_2 = v_1 \pm 4 = 512 \text{ Hz} \pm 4 = 516 \text{ Hz}$  or  $508 \text{ Hz}$



Increase in the tension of a piano string increases its frequency.

If  $v_2 = 516 \text{ Hz}$ , further increase in  $v_2$ , resulted in an increase in the beat frequency. But this is not given in the question.

If  $v_2 = 508 \text{ Hz}$ , further increase in  $v_2$  resulted in decrease in the beat frequency. This is given in the question. When the beat frequency decreases to 2 beats per second. Therefore, the frequency of the piano string before increasing the tension was 508 Hz.

29. (a) :  $l_1 = 0.516 \text{ m}$ ,  $l_2 = 0.491 \text{ m}$ ,  $T = 20 \text{ N}$ .

Mass per unit length,  $\mu = 0.001 \text{ kg/m}$ .

$$\text{Frequency, } v = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$$

$$v_1 = \frac{1}{2 \times 0.516} \sqrt{\frac{20}{0.001}}$$

$$v_2 = \frac{1}{2 \times 0.491} \sqrt{\frac{20}{0.001}}$$

$\therefore$  Number of beats =  $v_1 - v_2 = 7$ .

30. (b) : Car is the source and the hill is observer.

Frequency heard at the hill,  $v_1$

$$\therefore v_1 = \frac{v \times v}{(v - V)} = \frac{600 \times 330}{330 - 30}$$

Now for reflection, the hill is the source and the driver the observer.

$$\therefore v_2 = v_1 \times \frac{(330+30)}{330}$$

$$\Rightarrow v_2 = \frac{600 \times 330}{300} \times \frac{360}{330} \Rightarrow v_2 = 720 \text{ Hz.}$$

31. (c) : Amplitude = 2 cm = 0.02 m,  $v = 128$  m/s

$$\lambda = \frac{4}{5} = 0.8 \text{ m; } v = \frac{128}{0.8} = 160 \text{ Hz}$$

$$\omega = 2\pi v = 2\pi \times 160 = 1005; \quad k = \frac{2\pi}{\lambda} = \frac{2\pi}{0.8} = 7.85$$

$$\therefore y = 0.02 \sin(7.85x - 1005t).$$

32. (b) :  $x = a \sin(\omega t + \pi/6)$

$$\frac{dx}{dt} = a\omega \cos(\omega t + \pi/6)$$

Max. velocity =  $a\omega$

$$\therefore \frac{a\omega}{2} = a\omega \cos(\omega t + \pi/6);$$

$$\therefore \cos(\omega t + \pi/6) = \frac{1}{2}$$

$$60^\circ \text{ or } \frac{2\pi}{6} \text{ radian} = \frac{2\pi}{T} \cdot t + \pi/6;$$

$$\frac{2\pi}{T} \cdot t = \frac{2\pi}{6} - \frac{\pi}{6} = +\frac{\pi}{6}$$

$$\therefore t = +\frac{\pi}{6} \times \frac{T}{2\pi} = \left| +\frac{T}{12} \right|$$

33. (b) : Other factors such as  $\omega$  and  $v$  remaining

the same,  $I = A^2 \times \text{constant } K$ , or  $A = \sqrt{\frac{I}{K}}$

On superposition

$$A_{\max} = A_1 + A_2 \text{ and } A_{\min} = A_1 - A_2$$

$$\therefore A_{\max}^2 = A_1^2 + A_2^2 + 2A_1A_2$$

$$\Rightarrow \frac{I_{\max}}{K} = \frac{I_1}{K} + \frac{I_2}{K} + \frac{2\sqrt{I_1I_2}}{K}$$

$$A_{\min}^2 = A_1^2 + A_2^2 - 2A_1A_2$$

$$\Rightarrow \frac{I_{\min}}{K} = \frac{I_1}{K} + \frac{I_2}{K} - \frac{2\sqrt{I_1I_2}}{K}$$

$$\therefore I_{\max} + I_{\min} = 2I_1 + 2I_2$$

34. (a) :  $y = 0.25 \sin(10\pi x - 2\pi t)$

$$y_{\max} = 0.25$$

$$k = \frac{2\pi}{\lambda} = 10\pi \Rightarrow \lambda = 0.2 \text{ m}$$

$$\omega = 2\pi f = 2\pi \Rightarrow f = 1 \text{ Hz}$$

The sign is negative inside the bracket. Therefore this wave travels in the positive  $x$ -direction.

35. (b) :  $Y_1 = 4 \sin 500\pi t$ ,  $Y_2 = 2 \sin 506\pi t$

$$\omega_1 = 500\pi, \omega_2 = 2\pi v, v_1 = 250, v_2 = 253$$

$$v = v_2 - v_1 = 253 - 250 = 3 \text{ beats/s.}$$

$$\text{Number of beats per minute} = 3 \times 60 = 180.$$

36. (a) : Frequency =  $\frac{\text{velocity}}{\text{wavelength}}$

$$\therefore v_1 = \frac{v}{\lambda_1} = \frac{330}{5} = 66 \text{ Hz}$$

$$\text{and } v_2 = \frac{v}{\lambda_2} = \frac{330}{5.5} = 60 \text{ Hz}$$

$$\text{Number of beats per second} = v_1 - v_2 = 66 - 60 = 6.$$

37. (b) : Reverberation time,  $T = \frac{0.61 V}{aS}$

where  $V$  is the volume of room in cubic metres,  $a$  is the average absorption coefficient of the room,  $S$  is the total surface area of room in square metres.

$$\text{or, } T \propto \frac{V}{S}$$

$$\text{or, } \frac{T_1}{T_2} = \left( \frac{V_1}{V_2} \right) \left( \frac{S_2}{S_1} \right) = \left( \frac{V}{8V} \right) \left( \frac{4S}{S} \right) = \frac{1}{2}$$

$$\text{or, } T_2 = 2T_1 = 2 \times 1 = 2 \text{ sec. } (\because T_1 = 1 \text{ sec})$$

38. (a) :  $y(x, t) = 8.0 \sin(0.5\pi x - 4\pi t - \frac{\pi}{4})$

Compare with a standard wave equation,

$$y = a \sin \left( \frac{2\pi x}{\lambda} - \frac{2\pi t}{T} + \phi \right)$$

$$\text{we get } \frac{2\pi}{\lambda} = 0.5\pi \text{ or, } \lambda = \frac{2\pi}{0.5\pi} = 4 \text{ m.}$$

$$\frac{2\pi}{T} = 4\pi \text{ or, } T = \frac{2\pi}{4\pi} = \frac{1}{2} \text{ sec.}$$

$$v = 1/T = 2 \text{ Hz.}$$

Wave velocity,  $v = \lambda v = 4 \times 2 = 8$  m/sec.

39. (c) : Light waves are electromagnetic waves.

Light waves are transverse in nature and do not require a medium to travel, hence they can travel in vacuum. Sound waves are longitudinal waves and require a medium to travel. They do not travel in vacuum.

40. (c) :  $d_1 = 2$  m,  $d_2 = 3$  m

$$\text{Intensity} \propto \frac{1}{(\text{distance})^2}$$

$$I_1 \propto \frac{1}{2^2} \text{ and } I_2 \propto \frac{1}{3^2}$$

$$\therefore \frac{I_1}{I_2} = \frac{9}{4}$$

41. (a) :  $y_1 = 10^{-6} \sin[100t + (x/50) + 0.5]$   
 $y_2 = 10^{-6} \cos[100t + (x/50)]$

$$\begin{aligned} & \text{[using } \cos x = \sin(x + \pi/2)] \\ & = 10^{-6} \sin[100t + (x/50) + \pi/2] \\ & = 10^{-6} \sin[100t + (x/50) + 1.57] \end{aligned}$$

The phase difference =  $1.57 - 0.5 = 1.07$

[or using  $\sin x = \cos(\pi/2 - x)$ . We get the same result.]

**42. (b)** : 1st the car is the source and at the cliff, one observes  $f'$ .

$$\therefore f' = \frac{v}{v - v_s} f$$

2<sup>nd</sup> cliff is now source. It emits frequency  $f'$  and the observer is now the driver who observes  $f''$ .

$$\therefore f'' = \left[ \frac{v + v_o}{v} \right] f' \quad \text{or} \quad 2f = \left[ \frac{v + v_o}{v - v_s} \right] f$$

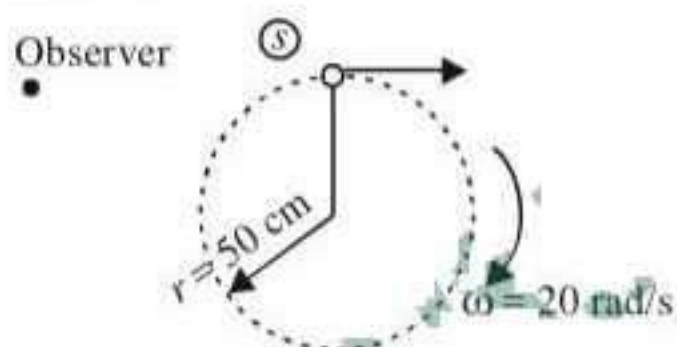
$$\Rightarrow 2v - 2v_o = v + v_o \quad \text{[as } v_s = v_o]$$

$$\Rightarrow v_o = \frac{v}{3}$$

$$\begin{aligned} \mathbf{43. (b)} : \text{ Apparent frequency, } f' &= \frac{v + v_o}{v} f \\ &= \frac{v + (1/5)v}{v} f = 1.2f \end{aligned}$$

Wavelength does not change by motion of observer.

**44. (b)** : The whistle is revolving in a circle of radius 50 cm. So the source (whistle) is moving and the observer is fixed.



The minimum frequency will be heard by the observer when the linear velocity of the whistle (source) will be in a direction as shown in the figure, i.e. when the source is receding.

The apparent frequency heard by the observer is then

$$\text{given by } v' = v \left[ \frac{v}{V + v} \right]$$

where  $V$  and  $v$  are the velocities of sound and source respectively and  $v$  is the actual frequency.

$$\text{Now, } v = r\omega = 0.5 \times 20 = 10 \text{ m/s}$$

$$V = 340 \text{ m/s, } v = 385 \text{ Hz.}$$

$$\therefore v' = 385 \times \frac{340}{340 + 10} = 374 \text{ Hz.}$$

**45. (c)** : The equation of progressive wave travelling in positive x-direction is given by

$$y = a \sin \frac{2\pi}{\lambda} (vt - x)$$

Here  $a = 0.2 \text{ m}$ ,  $v = 360 \text{ m/sec}$ ,  $\lambda = 60 \text{ m}$

$$\therefore y = 0.2 \sin \frac{2\pi}{60} (360t - x) = 0.2 \sin \left[ 2\pi \left( 6t - \frac{x}{60} \right) \right]$$

**46. (c)** : Comparing the given equation with general equation,  $y = a \sin 2\pi \left( \frac{t}{T} - \frac{x}{\lambda} \right)$ , we get

$$T = \frac{2\pi}{100} \quad \text{and} \quad \lambda = 20\pi$$

$$\therefore v = v\lambda = \frac{100}{2\pi} \times 20\pi = 1000 \text{ m/s.}$$

**47. (b)** : Resultant amplitude =  $2a(1 + \cos\phi) = a$

$$\therefore (1 + \cos\phi) = 1/2; \quad \cos\phi = -\frac{1}{2}; \quad \phi = \frac{2\pi}{3}$$

$$\mathbf{48. (c)} : n = \frac{1}{2l} \sqrt{\frac{T}{\pi r^2 \rho}}$$

$$\rho'_1 = \frac{\rho}{2}; \quad T' = 2T \quad \text{and} \quad D' = 2D \quad \text{or} \quad r' = 2r$$

$$n' = \frac{1}{2l} \sqrt{\frac{2T}{\pi(2r)^2 \frac{\rho}{2}}}$$

$$\text{After solving, } n' = \frac{1}{2l} \sqrt{\frac{T}{\pi r^2 l}} = n.$$

**49. (b)** : Given :  $x = a \cos(\omega t + \delta)$

$$\text{and } y = a \cos(\omega t + \alpha) \quad \dots (i)$$

where  $\delta = \alpha + \pi/2$

$$\begin{aligned} \therefore x &= a \cos(\omega t + \alpha + \pi/2) \\ &= -a \sin(\omega t + \alpha) \quad \dots (ii) \end{aligned}$$

Given the two waves are acting in perpendicular direction with the same frequency and phase difference  $\pi/2$ .

From equations (i) and (ii),

$$x^2 + y^2 = a^2$$

which represents the equation of a circle.

**50. (a)** : As  $n \propto (1/l)$  and  $l = l_1 + l_2 + l_3$

$$\therefore \frac{1}{n} = \frac{1}{n_1} + \frac{1}{n_2} + \frac{1}{n_3}$$

$$\mathbf{51. (a)} : f' = \frac{v - u}{v} f; \quad f'' = \frac{v + u}{v} f$$

$$\text{Number of beats} = f'' - f' = \frac{2u}{\lambda}$$

**52. (c)** : Number of beats produced per second,

$$= v_1 - v_2 = \frac{v}{\lambda_1} - \frac{v}{\lambda_2}$$

$$12 = v \left[ \frac{1}{50} - \frac{1}{51} \right] \quad \text{or} \quad 12 = \frac{v \times 1}{50 \times 51}$$

$$\text{or, } v = 12 \times 50 \times 51 \text{ cm/s} = 306 \text{ m/s.}$$

**53. (d)** : The given equation of wave is

$$y = y_0 \sin \frac{2\pi}{\lambda} (vt - x)$$

$$\text{Particle velocity} = \frac{dy}{dt} = y_0 \cos \frac{2\pi}{\lambda} (vt - x) \frac{2\pi v}{\lambda}$$

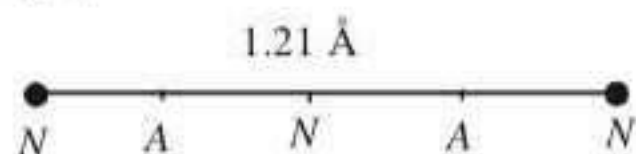
$$\left(\frac{dy}{dt}\right)_{\max} = y_0 \frac{2\pi}{\lambda} v$$

$$\therefore y_0 \frac{2\pi}{\lambda} v = 2v \quad \text{or} \quad \lambda = \pi y_0$$

$$\begin{aligned} 54. \text{ (b) : } n' &= n + n_1 = \frac{nv}{v - v_s \cos \theta} \\ &= \frac{nv}{v} \quad [\because \cos 90^\circ = 0] \end{aligned}$$

$$n' = n \quad \therefore n_1 = 0$$

55. (c) : Distance between a node and adjoining antinode =  $\lambda/4$



From figure, distance between two atoms

$$= 4 \times \frac{\lambda}{4} = 1.21 \text{ \AA} \quad \text{or} \quad \lambda = 1.21 \text{ \AA}$$

56. (c) : Displacement,  $Y_{\max} = a$ ,  $Y_{\min} = 0$

Time taken =  $T/4$

$$\therefore T/4 = 0.170 \quad \therefore T = 0.68$$

The frequency of wave =  $1/T = 1.47 \text{ Hz}$

57. (a) : The frequency of standing wave,

$$\begin{aligned} v &= \frac{n}{2l} v \\ &= \frac{5 \times 20}{2 \times 10} = 5 \text{ Hz} \end{aligned}$$

58. (d) : For the cylindrical tube open at both ends,  $f = v/2l$ .

When half of the tube is in water, it behaves as a closed pipe of length  $l/2$ .

$$\therefore f' = \frac{v}{4(l/2)} = \frac{v}{2l} \quad \therefore f' = f$$

59. (c) : Sound wave equation is

$$y = 0.0015 \sin(62.4x + 316t)$$

Comparing it with the general equation of motion

$$y = A \sin 2\pi \left[ \frac{x}{\lambda} + \frac{t}{T} \right], \text{ we get } \frac{2\pi}{\lambda} = 62.4$$

$$\text{or } \lambda = \frac{2\pi}{62.4} = 0.1 \text{ unit.}$$

60. (a) : Phase difference  $\theta = 60^\circ = \frac{\pi}{3} \text{ rad.}$

$$\text{Phase difference } (\theta) = \frac{\pi}{3} = \frac{2\pi}{\lambda} \times \text{Path difference.}$$

$$\text{Therefore path difference} = \frac{\pi}{3} \times \frac{\lambda}{2\pi} = \frac{\lambda}{6}$$

61. (a) : Length of sonometer wire ( $l$ ) = 110 cm and ratio of frequencies = 1 : 2 : 3.

$$\text{Frequency } (v) \propto \frac{1}{l} \quad \text{or} \quad l \propto \frac{1}{v}$$

$$\text{Therefore } AC : CD : DB = \frac{1}{1} : \frac{1}{2} : \frac{1}{3} = 6 : 3 : 2$$

$$\text{Therefore } AC = 6 \times \frac{110}{11} = 60 \text{ cm and}$$

$$CD = 3 \times \frac{110}{11} = 30 \text{ cm.}$$

$$\text{Thus } AD = 60 + 30 = 90 \text{ cm.}$$

62. (c) : Frequency ( $v$ ) = 4.2 MHz =  $4.2 \times 10^6 \text{ Hz}$  and speed of sound ( $v$ ) = 1.7 km/s =  $1.7 \times 10^3 \text{ m/s}$ .

$$\begin{aligned} \text{Wave length of sound in tissue } (\lambda) &= \frac{v}{\nu} = \frac{1.7 \times 10^3}{4.2 \times 10^6} \\ &= 4 \times 10^{-4} \text{ m.} \end{aligned}$$

63. (a) : Frequency of first source with 5 beats/sec = 100 and frequency of second source with 5 beats/sec = 205. The frequency of the first source =  $100 \pm 5 = 105$  or 95 Hz.

Therefore frequency of second harmonic source = 210 Hz or 190 Hz.

As the second harmonic gives 5 beats/second with the sound of frequency 205 Hz, therefore frequency of second harmonic source should be 210 Hz. The frequency of source = 105 Hz.

64. (a) : Wavelength ( $\lambda$ ) = 5000 Å and velocity ( $v$ ) =  $1.5 \times 10^4 \text{ m/s}$ .

$$\begin{aligned} \text{Wavelength of the approaching star, } (\lambda') &= \lambda \frac{c-v}{c} \quad \text{or} \\ \frac{\lambda'}{\lambda} &= 1 - \frac{v}{c} \end{aligned}$$

$$\text{or, } \frac{v}{c} = 1 - \frac{\lambda'}{\lambda} = \frac{\lambda - \lambda'}{\lambda} = \frac{\Delta \lambda}{\lambda}$$

$$\text{Therefore } \Delta \lambda = \lambda \times \frac{v}{c} = 5000 \text{ \AA} \times \frac{1.5 \times 10^6}{3 \times 10^8} = 25 \text{ \AA}$$

(where  $\Delta \lambda$  is the change in the wavelength)

65. (a, b) : (a) represents a harmonic progressive wave in the standard form where as (b) also represents a harmonic progressive wave, both travelling in the positive  $x$ -direction. In (b),  $a$  is the angular velocity,  $\omega$  and  $b$  is  $k$ ;  $c$  is the initial phase.

(d) represents only S.H.M.

66. (a) : Frequency ( $v$ ) = 100 Hz and distance from fixed end = 10 cm = 0.1 m. When a stationary wave is produced, the fixed end behaves as a node. Thus wavelength ( $\lambda$ ) =  $2 \times 0.1 = 0.2 \text{ m}$ .

$$\text{Therefore velocity } v = v\lambda = 100 \times 0.2 = 20 \text{ m/s.}$$

67. (a) :  $y = A \sin(100t) \cos(0.01x)$ . Comparing it with standard equation

$$y = A \sin\left(\frac{2\pi}{T}t\right) \cos\left(\frac{2\pi}{\lambda}x\right),$$

we get  $T = \frac{\pi}{50}$  and  $\lambda = 200\pi$ .

Therefore velocity,  $v = \frac{\lambda}{T} = \frac{200\pi}{\pi/50} = 200 \times 50$   
 $= 10000 = 10^4$  m/s.

68. (a) : First case: Frequency =  $\nu$ ;

No. of beats/sec. = 5 and

frequency (sounded with) = 200 Hz.

Second case: Frequency =  $2\nu$ ; No. of beats/sec = 10 and frequency (sounded with) = 420 Hz.

In the first case, frequency ( $\nu$ ) =  $200 \pm 5 = 205$

or 195 Hz. And in the second case, frequency ( $2\nu$ ) =  $420 \pm 10$

or  $\nu = 210 \pm 5 = 205$  or 215. So common value of  $\nu$  in both the cases is 205 Hz.

69. (c) : Beats are produced. Frequency of beats will be  $\frac{1}{3} - \frac{1}{4} = \frac{1}{12}$ . Hence time period = 12 s.

70. (c) :  $f = \frac{1}{2l} \left[ \frac{T}{\mu} \right]^{\frac{1}{2}}$  when  $f$  is halved, the length is doubled

$\therefore$  Length is 1 m.

71. (c) : Velocity of sound  $v \propto \sqrt{T}$

$\therefore \frac{v}{2v} = \frac{\sqrt{273+27}}{\sqrt{T}}$  or  $T = 1200 \text{ K} = 927^\circ\text{C}$

72. (b) : For production of beats different frequencies are essential. The different amplitudes effect the minimum and maximum amplitude of the beats. If frequencies are different, phases will be different.

73. (d) : Compare with the equation

$$y = a \cos(2\pi\nu t + \phi)$$

This give  $2\pi\nu = 2000$

$$\nu = \frac{1000}{\pi} \text{ Hz}$$

74. (b) : With the propagation of a longitudinal wave, energy alone is propagated.

75. (a) : Here  $v' = \frac{9}{8}v$

Source and observer are moving in opposite direction, apparent frequency

$$v' = v \times \frac{(v+u)}{(v-u)}$$

$$\frac{9}{8}v = v \times \frac{340+u}{340-u}$$

$$\Rightarrow 9 \times 340 - 9u = 8 \times 340 + 8u$$

$$\Rightarrow 17u = 340 \times 1 \Rightarrow u = \frac{340}{17} = 20 \text{ m/s}$$

76. (d) : Third overtone has a frequency  $4n$ , 4<sup>th</sup> harmonic = three full loops + one half loop, which would make four nodes and four antinodes.



77. (c) : From  $\Delta x = \frac{\lambda}{2\pi} \Delta\phi$ ,

$$\lambda = 2\pi \frac{\Delta x}{\Delta\phi} = \frac{2\pi(0.4)}{1.6\pi} = 0.5 \text{ m}$$

$$\nu = \frac{v}{\lambda} = \frac{330}{0.5} = 660 \text{ Hz}$$

78. (a) :  $\mu = \frac{0.035}{5.5}$  kg/m,  $T = 77$  N

where  $\mu$  is mass per unit length.

$$v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{77 \times 5.5}{0.035}} = 110 \text{ m/s}$$

79. (c) : Intensity  $\propto (\text{amplitude})^2$  and also intensity  $\propto (\text{frequency})^2$ . Therefore original  $I \propto A^2\omega^2$

$$I' \propto 4A^2 \frac{\omega^2}{16} \text{ i.e., } \frac{1}{4}I$$

80. (b) : Velocity of sound in any gas depends upon density and elasticity of gas.

$$v = \sqrt{\frac{\gamma P}{\rho}} \text{ or } \sqrt{\frac{B}{\rho}}$$

81. (b) : The standard equation of a progressive wave is

$$y = a \sin\left[2\pi\left(\frac{t}{T} - \frac{x}{\lambda}\right) + \phi\right]$$

The given equation can be written as

$$y = 4 \sin\left[2\pi\left(\frac{t}{10} - \frac{x}{18}\right) + \frac{\pi}{6}\right]$$

$\therefore a = 4$  cm,  $T = 10$  s,

$\lambda = 18$  cm and  $\phi = \pi/6$ .

